

1 Head Count

Consider a coin with $\mathbb{P}(\text{Heads}) = 2/5$. Suppose you flip the coin 20 times, and define X to be the number of heads.

(a) What is the distribution of X ?

(b) What is $\mathbb{P}(X = 7)$?

(c) What is $\mathbb{P}(X \geq 1)$?

(d) What is $\mathbb{P}(12 \leq X \leq 14)$?

2 Telebears

Lydia has just started her CalCentral enrollment appointment. She needs to register for a marine science class and CS 70. There are no waitlists, and she can attempt to enroll once per day in either class or both. The CalCentral enrollment system is strange and picky, so the probability of enrolling in the marine science class is μ and the probability of enrolling in CS 70 is κ . These events are independent. Let M be the number of days it takes to enroll in the marine science class, and C be the number of days it takes to enroll in CS 70.

(a) What distribution do M and C follow? Are M and C independent?

(b) For some integer $k \geq 1$, what is $\mathbb{P}[C \geq k]$?

- (c) For some integer $k \geq 1$, what is the probability that she is enrolled in both classes before day k ?

3 Fishy Computations

Use the Poisson distribution to answer these questions:

- (a) Suppose that on average, a fisherman catches 20 salmon per week. What is the probability that he will catch exactly 7 salmon this week?
- (b) Suppose that on average, you go to Fisherman's Wharf twice a year. What is the probability that you will go at most once in 2018?
- (c) Suppose that in March, on average, there are 5.7 boats that sail in Laguna Beach per day. What is the probability there will be *at least* 3 boats sailing throughout the *next two days* in Laguna?

4 Combined Head Count

- (a) What is the sample space Ω generated from these flips?
- (b) Define a random variable X to be the number of heads. What is the distribution of X ?
- (c) Define a random variable Y to be 1 if $\omega = (H, T)$ and 0 otherwise. What is the distribution of Y ?
- (d) Define a third random variable $Z = X + Y$. What is the distribution of Z ?